YoUSSEF COURBAGE ANI) PIHILIPPEFARGUES*

## INTRODICTION

In commeries in which population data are still defective, demographers have paid little attention to vital statistics. ${ }^{1}$ Brass attributes this lack of interest to the absence of a theoretical model adapted to the analysis of these data. ${ }^{2}$

Yet, incomplete vital registration records may well yield a fairly accurate estimation of the main mortality indicators, such as life tables or crude death rates. A first attempt was made, some years ago, to improve the health statistics of Lebanon. ${ }^{3}$ This method, which relied on the life tables of a certain number of countries was later complemented by using Princeton model life tables. ${ }^{4}$ This method, which gave very similar results to those obtained by the previous one, was successfully applied to the data of two other comntries, Jordan ${ }^{5}$ and Libya ${ }^{6}$. In this paper we illustrate the diffetent stages of this method by applying them to data relating to the Malagasy Republic

In many developing countries efforts have recently been devoted to the implementation or improvement of the registration of vital events. ${ }^{7}$ The construction of appropriate methods for processing such data is, therefore, of considerable importance. As no special surveys are required no additional costs are incurred. Moreover, the procedure has the advantage over other methods of adjustment that no assumptions are required relating to stability or quasi-stability of the population or constancy of mortality in the recent past.

The general principle of the method will be briefly explained before applying it to Malagasy data.

## PRINCIPIES AND ASSUMPTIONS

Underregistration of deaths is common in vital registration systems in many developing countries Moreover, early childhood deaths are less completely registered than those at older ages everywhere for when births escape registration subsequent deaths are likely to do so as well. Yet, above a certain age ${ }^{8}$ when births are no longer registered, there is no reason why the completeness of death registration should depend on the age at death. Our first assumption is thus, that there exists an age beyond which the rate of underregistration of deaths does not vary significantly. ${ }^{9}$ In other

[^0]words, above this age the age distribution of registered deaths differs only very shghtly from the actual (but unknown) age distribution of deaths.

Moreover, any decrease in mortality in a population normally consists of a shift towards older ages of deaths previously occurring at younger ages. Thus, for a given age structure of the population, a fall in mortality leads to a concentration of deaths at older ages. For a given population age structure, the age structure of deaths and the level of mortality are related.

A second assumption, which will be discussed in detail later, is that the age structure of deaths of the country under study is similar to a set of standard age-specific death rates. ${ }^{10}$

These assumptions are later combined and provide the basis of the method: a knowledge of the distribution of deaths by age, and of a family of life tables to which this distribution could be related, makes it possible to deduce the true level of mortality (measured by the death rate above a given age) from the relation between age structure of deaths and level of mortality. This true level. is then compared with registered mortality, thus making possible an estimate of the extent of underregistration of deaths, and a later adjusiment of observed age-specific death rates, as the overall underregistration rate applies to each individual age group.

BASIC DATA REQUIRED
Two serics of data are required:
(1) Death statistics by age obtained either from vital registration records or from a census or survey in which questions on vital events taking place within the last twelve months are included.
(2) The age and sex distribution of the population.

Table 1. Registered deaths in Madagascar (1965-67)

| Age group | 1965 |  | 1966 |  | 1967 |  | Average 196.5-6,7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Males | Iemales | Males | Females | Males | Females | Males | females |
| 0 | 7,355 | 6,307 | 8,836 | 7,561 | 9.620 | 8,152 | 8.604 | 7.340 |
| 1-4 | 6.263 | 6.223 | 8,361 | 7,808 | 8.635 | 8.356 | 7.753 | 7.462 |
| 5-9 | 1,403 | 1,273 | 1,947 | 1,722 | 2,045 | 1,857 | 1.798 | 1.617 |
| 10-14 | 770 | 632 | 922 | 825 | 1,111 | 957 | 934 | 805 |
| 15-19 | 758 | 846 | 908 | 999 | 962 | 1,102 | 876 | 982 |
| 20-24 | 747 | 934 | 786 | 1,036 | 805 | 1,056 | 779 | 1.009 |
| 25-29 | 850 | 1,309 | 902 | 1,405 | 957 | 1.364 | 903 | 1,359 |
| 30-34 | 883 | 1,076 | 968 | 1,290 | 950 | 1.234 | 934 | 1.200 |
| 35-39 | 1,142 | 1.214 | 1,291 | 1,464 | 1,086 | 1,292 | 1,173 | 1.323 |
| 40-44 | 1,129 | 1,114 | 1,316 | 1.313 | 1,308 | 1,184 | 1.251 | 1.204 |
| 45-49 | 1,452 | 1.256 | 1,771 | 1.506 | 1,626 | 1,410 | 1.616 | 1.391 |
| 50-54 | 1,595 | 1,172 | 1,914 | 1.649 | 1.642 | 1,501 | 1.717 | 1.441 |
| 55-59 | 1,655 | 1.257 | 2,177 | 1,620 | 2,087 | 1,495 | 1.973 | 1.457 |
| 60-66 | 1,857 | 1,509 | 2,174 | 1.865 | 1,834 | 1.610 | 1.955 | 1.661 |
| 65-69 | 1.710 | 1,308 | 2,471 | 1,849 | 2.221 | 1,717 | 2.134 | 1.625 |
| $70+$ | 4.812 | 4.601 | 6.452 | 6,504 | 5.523 | 5.610 | 5.596 | 5.572 |
| Unknown* | 431 | 338 | 352 | 300 | 282 | 224 | 355 | 287 |
| Total | 34,812 | 32,369 | 43,548 | 40,716 | 42.694 | 40.121 | 40.351 | 37.735 |

Source: Institut National de la Statistique et de la Recherche Economique, Inventaire Socio-economique. tome I (Tananarive, 1969).

* Deaths of unknown age were omitted in further calculations.
that the assumption holds: the pattern of the mortality rates thus obtained does not differ greatly from those of existing life tables.
${ }^{10}$ This condition is very flexible. It is sufficient to find a family of age-specific death rates in which the age distribution of deaths in the population studied in two large age groups (e.g. 1-50 years and 50 years and over, or 5-60 years and 60 years and over). for a given death rate above a certain age (e.g. one year or five years) is close to that which would have been observed if mortality had followed the selected pattern exactly.

Table 2. Age and sex distribution of the population in Madagascar in 1960 (in thousands)

| Age group | Males | liemales | Age group | Males | Iemales |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 133 | 132 | 40-44 | 133 | 141 |
| 1-4 | 432 | 430 | 45-49 | 125 | 127 |
| 5-9 | 484 | 456 | 50-54 | 106 | 98 |
| 10-14 | 428 | 387 | 55-59 | 84 | 89 |
| 15-19 | 269 | 301 | 60-64 | 60 | 54 |
| 20-24 | 193 | 227 | 65-69 | 51 | 46 |
| 25-29 | 163 | 230 | 70 + | 76 | 72 |
| 30-34 | 156 | 179 | N.I). | 2 | 2 |
| 35-39 | 154 | 180 | Total | 3,049 | 3,151 |

Source: Institut National de la Statistique et de la Recherche Economique, Enquête demographique, Madagascar, 1966 (Tananarive. 1967).

Registered deaths should be sufficiently numerous to enable their age distribution to be accurately estimated. As an example, in Madagascar statistics on deaths were available for the three calendar years 1965-67. Hence, the calculations refer to the average number of deaths during these three years rather than to those of 1966 only - the year of the survey for which the age structure of the population is available. This averaging tends to minimize chance fluctuations and to avoid errors caused by shifting deaths from one year to another.

The age distribution of the population should be given for the middle of the period for which death statistics are available. If it is not given, any reliable age distribution can be projected to the middle of that period. Moreover, age pyramids are often distorted because of age mis-statement. But as mis-statements of age are likely to affect deaths as well as the enumerated population, it seems preferable not to adjust the age structure. But, if the final series of rates obtained from these calculations seems biased, an adjustment of the age structure may well become necessary. ${ }^{11}$

## A DETAILED EXAMPLE OI THE METHOH

Notation:

| Registered deaths | $D^{\prime}$ |
| :--- | :--- |
| Actual deaths | $D$ |
| Population | $P$ |
| Registered death rate | $m^{\prime}$ |
| Actual death rate | $m$ |
| Closed age group | $(x, x+a)$ |
| Open age group | $(x+)$ |

Any age-specific death rate can be written:

$$
\begin{equation*}
m(x, x+a)=\frac{D(x, x+a)}{P(x, x+a)}=\frac{P(a+)}{P(x, x+a)} \cdot \frac{D(x, x+a)}{D(a+)} \cdot \frac{D(a+)}{P(a+)} \tag{1}
\end{equation*}
$$

Thus, the age-specific death rate is the product of three factors:
(1) The proportion in the age group $(x, x+a)$ of the population aged $a$ and over $(x \geq a)$, where $a$

[^1]is a young ape used as a lower limit in subsequent calculations. This propertom is knewn since a reliable age-sex distribution of the population is available.
(2) The proportion of deaths at ages $(x, x+a)$ among total deaths aged $a$ or over. 1 hus proportion can be estimated by the proportion:
$$
\frac{D^{\prime}(x, x+a)}{D^{\prime}(a+1}
$$
by virtue of the assumption of a constant rate of underregistration of deaths at ages above $\alpha$.
(3) The death rate of the open age interval $a$ and over. The method of estimating this ratio is shown below.

The rate $m(a+)$ is unknown since the registered rate $m^{\prime}(a+)$ is obvlously underestimated. ${ }^{12}$ and is a measure of the level of mortality in this age group. For a given population age structure there is a relation between this mortality level and the age distribution of deaths beyond age $a$. This last quantity may be represented by a single index, which measures the concentration of deaths at older ages:

$$
i(a, \beta)=\frac{D(\beta+)}{D(a+)}
$$

where $\beta$ is an advanced age used as the second limit in the subsequent calculations. According to our first assumption $i(\alpha, \beta)$ can be estimated by the ratio:

$$
\frac{D^{\prime}(\beta+)}{D^{\prime}(a+)}
$$

In the case of Madagascar, two values have been used for each one of the two thresholds a and $\beta$ : $a=1$ and 5 years and $\beta=50$ and 60 years. The are thus four possible values of $i(a, \beta)$.

It remains to find out which level of death rate at ages above $a$ corresponds to a given index $i(a, \beta)$. Existing life tables will be used as a standard pattern for this estimation.

For each sex, separately, the age-specific death rates of several life tables are applied to the

Table 3. Index of concentration $\mathrm{i}(a, \beta)$ of deaths at older ages: Madagascar (1965-67)

| $i(a . \beta)$ | Males | Females |
| :--- | :--- | ---: |
| $i(1.50)$ | 0.4261 | 0.3905 |
| $i(1,60)$ | 0.3085 | 0.2942 |
| $i(5,50)$ | 0.5658 | 0.5191 |
| $i(5.60)$ | 0.4097 | 0.3912 |
|  |  |  |

Source: Computed from Table 1.

[^2]| $a$ | Males | Females |
| :--- | ---: | ---: |
| 1 year | 10.8 | 10.0 |
| 5 years | 9.5 | 8.7 |

$\Gamma_{\text {able }}+1$ alues of $\mathrm{m}(a+)($ per thousand $/$ and $\mathrm{i}(a, \beta)$ associated with the age structure of the population in Madagascar and death rates of the Princeton life tables, Model 'West' (males)

| Level | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $m(1-1$ | 26.52 | 24.42 | 22.50 | 20.74 | 19.12 | 17.63 | 16.23 | 14.94 | 13.60 | 12.51 | 11.46 |
| 11! 501 | 0.3563 | 0.3663 | 0.3772 | 0.3890 | 0.4018 | 0.4157 | 0.4310 | 0.4478 | 0.4700 | 0.4922 | 0.5183 |
| 11. 601 | 0.2552 | 0.2645 | 0.2746 | 0.2855 | 0.2974 | 0.3104 | 0.3246 | 0.3403 | 0.3607 | 0.3804 | 0.4043 |
| m15-1 | 22.40 | 20.84 | 19.40 | 18.09 | 16.87 | 15.73 | 14.68 | 13.70 | 12.73 | 11.97 | 11.16 |
| 115.501 | 0.4952 | 0.5040 | 0.5134 | 0.5237 | 0.5348 | 0.5467 | 0.5596 | 0.5735 | 0.5894 | 0.6042 | 0.6252 |
| 115.601 | 0.3546 | 0.3638 | 0.3737 | 0.3844 | 0.3959 | 0.4082 | 0.4215 | 0.4358 | 0.4523 | 0.4674 | 0.4876 |

Source: Calculations in the Appendix.
appropiate populations of Madagascar. These calculations give, for cach life table, values i(a, $\beta$ ) and $m(a+)$, so that a set of mumerical correspondences between $i(a, \beta)$ and $m(a+)$ is obtained ${ }_{a} M_{x}$ is the age specific death rate of age group $(x, x+a)$ in a life tahle, then, separately for cach sex:

$$
\begin{gathered}
m(a+)=\sum_{x=a}^{\infty} P^{\prime}(x, x+a) M(x, x+a) \sum_{x=a}^{\infty} P(x, x+a) \\
i(a, \beta)=\sum_{x=\rho}^{\infty} P(x, x+a) M(x, x+a) \sum_{x=a}^{\infty} P(x, x+a) M(x, x+a)
\end{gathered}
$$

The products ${ }_{a} P_{x} \cdot{ }_{a} M_{x}$ are the deaths which would have occurred in age group $(x, x+a)$ in Madagascar if the central age-specific death rates of the life table had applied. We have used the rates of the Princeton Model 'West' life tables from level 5 to 15 . The results for men only are presented in Table 4. For women, exactly the same method was used.

The results of Table 4 can be represented graphically. Four nomograms are thus obtained showing a perfect one-one correspondence between the level measured by $m(a+)$, and the structure of mortality measured by $i(a, \beta)$. Since $i(a, \beta)$ can be directly deduced from the registered deaths of a given population by reading off the value on the nomogram, the death rate $m(a+)$ corresponding to the index of concentration of deaths at older ages in this population may be obtained. ${ }^{13}$ The amount of underregistration of deaths above age $a$ and the correction factor can then be deduced.

In the Madagascar example, this calculation was performed for each of the four values $i(a, \beta)$. Two of the correction factors relate to deaths over the age of one year, and two to deaths over the age of five years. However, the underregistration rate, and, therefore, the correction factor for a given sex, vary very little with the thresholds $a$ and $\beta$. In our example, the correction factor does not change perceptibly, whether we take $a=1$ or $a=5$. It seems preferable, in this case, to choose $a=1$ in order to apply the adjustment to all deaths recorded as taking place at ages above one year. ${ }^{14}$

If we had chosen $a=5$ we would not have been able to adjust deaths in the age group 1-4. The choice of $\beta$, however, might affect the correction factor rather more. For $\beta=50$, the underregistration rates come out a little lower than if $\beta=60$, both for males and females. However, considering that age at death is more likely to be wrongly given for older persons, better results would be obtained for lower values of $\beta$; therefore $\beta$ was taken as 50 rather than 60 years. ${ }^{15}$

Thus, for Madagascar, we can estimate $m(1+)$ from the value of $i(1,50)$ derived from registered deaths. The correction factor finally obtained, is the ratio $m(1+) / m^{\prime}(1+)$. For males this factor is 1.54 and for females 1.34 .

The adjusted age-specific death rates can then be obtained by applying these correction factors to all age groups over one year: ${ }^{16}$

$$
\begin{aligned}
\text { Males }_{a} m_{x} & =1.54_{a} m_{x}^{\prime} \\
\text { Females }_{a} m_{x} & =1.34_{a} m_{x}^{\prime}
\end{aligned}
$$

${ }^{13}$ The construction of a nomogram for eleven levels of life tables is presented in this paper only to illustate the one-one correspondence between $m(a+1)$ and $i(a, \beta)$. In practice, the two levels of lite tables which enclose the values of $i(a, \beta)$ have to be found by trial and error and the value of $m(\alpha+)$ obtained by interpolation.
${ }^{14}$ In the case of Lebanon. on the other hand, the choice $a=5$ ycars seemed more appropriate.
${ }^{15} \mathrm{~K}$. Vaidyanathan, who has applied this method in an unpublished paper, has chosen a value of $\beta$ as low a 30 years, using $i(5,30)$ in: K. Vaidyanathan. 'A Simple Method for Estimation of Death Rate and Expectation of Life at Birth from Defective Registration Statistics', quoted by M. S. A. Issa op. cit. in footnote 6, p. 16.
${ }^{16}$ The relation ${ }_{a} m_{x}=m(1+) / m^{\prime}(1+)_{a} m_{x}^{\prime}$ is equivalent to Equation 1 in this section with $a=1$

$$
\text { (1) } \quad{ }_{a} m_{x}=\frac{P(1+)}{{ }_{a} P_{x}} \times \frac{{ }_{a} D_{x}}{D(1+)} \times \frac{D(1+)}{P(1+)} x \geq 1 \text { as }{ }_{a} D_{x} / D(1+)={ }_{a} D_{x}^{\prime} / D^{\prime}(1+) .
$$



Figure 1. Nomogram showing the relation between the index of concentration of deaths at older ages $i(a, \beta)$ and the overall death rate above age $a: m(a+)$

Table 5. Estimation of the level of mortality above age a and of the correction factor for registered deaths
$\left.\begin{array}{lccccc}\hline & & \text { Death rate at ages above } a\end{array}\right)$

Source: Adjusted rates are obtained from Table 4, registered rates from basic data of Tables 1 and 2.

We may write (1) as

$$
{ }_{a} m_{x}=\frac{P(1+)}{{ }_{a} P_{x}} \times \frac{a^{\prime} D_{x}^{\prime}}{D^{\prime}(1+)} \times \frac{D(1+)}{P(1+)}=a_{m^{\prime}} m_{x} \times\left\{m(1+) / m^{\prime}(1+)\right\} .
$$

It should be noted that. for ages over one, the classical formula for the conversion of central death rates into probabilities of dying:

$$
n q_{x}=\frac{-2 n}{2+n_{n} m_{x} m_{x}} \text { has becn used. }
$$

However the application of these correction factors to the registered death rates below one year of age yiclds results which are clearly too low:

$$
\begin{aligned}
\text { Males } & 1.54 \times 64.69=99.62 \\
\text { Females } & 1.34 \times 55.61=74.52
\end{aligned}
$$

These results are far below known levels of infant mortality in African countries which are close to or higher than 150. But, as infant deaths are likely to be less completely registered than deaths above one year of age, it scems preferable to deduce infant mortality rates from the l'rinceton life tables, considering the close connection between infant mortality rates and death rates in early childhood: hence $1 q_{0}$ is determined by interpolation between the two levels of the 'West tables which enclose the value of ${ }_{4} q_{1}$ found for Madagascar. Therefore, $1 q_{0}$ is the only rate which is directly derived from model life tables. ${ }^{17}$

## MAJOR FINDINGS

These calculations lead to the construction of the life tables of Madagascar 1965-67 (Table 6). These life tables may be compared with the Princeton models. But these sets were used only as standards for the estimation of the overall death rate (one year and above). This means that they merely determined a level of mortality. But the structure of these life tables depends only on the Madagascar data and is not affected by the use of model life tables.

Mortality rates in Madagascar for both sexes fluctuate about an average level in the model life tables (Level 10 for males, 11 for females). without greatly deviating from it. (Figure 2) The whole set of rates is enclosed within a narrow range: Levels 7 and 13, depending on age. This shows that the mortality structure given by this method is independent of that of model life tables: also that it is likely to yield true results. Differences observed between the mortality rates in Madagascar and those of the average level of the model life tables do not follow a regular pattern. If this were not so, it could indicate that underregistration of deaths depended upon age. The diagrams would then have shown age groups where all Madagascar mortality rates were higher than those of the average level, and others where they all were lower. The non-systematic character of these deviations tends to prove that the assumption that underregistration of deaths was independent of age is justified. ${ }^{\text {h }}$

The same method was applied to each sex separately. The consistency of the results of the two series of rates is worth noting: a male excess mortality at all ages but less acute between 15 and 40 years of age, because of increased mortality of women in the reproductive age groups. The difference between the average level of mortality for the two sexes (Level 10 for males and 11 for females) is due mainly to the female excess mortality between 5 and 20 years of age in the Princeton model life tables (Level 10, Model 'West'); there is no reason why such a pattern should exist in

[^3]Table 6. Abridged life tables by sex in Madagascar (1965-67)

| Age | Registered rates ${ }_{a} m_{x}^{\prime}$ | Adjusted rates $a_{x}$ | Mortality rates $a_{x}$ | $\begin{aligned} & \text { Survivors } \\ & l_{x} \end{aligned}$ | Deaths $a_{x}^{d_{x}}$ | Stationary population ${ }_{a} L_{x}$ | $\begin{aligned} & \text { Stationary } \\ & \text { population } \\ & T_{x} \end{aligned}$ | $\begin{gathered} \text { Life } \\ \text { expectancy } \\ \dot{e}_{x} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A.MALES |  |  |  |  |  |  |  |  |
| 0 | 64.69 | (220.18) $\dagger$ | (187.17)* | 10,000 | 1,872 | 8,502 | 407.151 | 40.72 |
| 1 | 17.95 | 27.64 | 104.77 | 8,128 | 851 | 30.810 | 398,649 | 49.05 |
| 5 | 3.72 | 5.73 | 28.25 | 7,277 | 206 | 35,870 | 367,839 | 50.55 |
| 10 | 2.18 | 3.36 | 16.66 | 7,071 | 118 | 35,061 | 331,969 | 46.95 |
| 15 | 3.26 | 5.02 | 24.79 | 6,953 | 172 | 34,336 | 296.908 | 42.70 |
| 20 | 4.04 | 6.22 | 30.62 | 6,781 | 208 | 33,386 | 262,572 | 38.72 |
| 25 | 5.54 | 8.53 | 41.76 | 6,573 | 274 | 32.180 | 229,186 | 34.87 |
| 30 | 5.99 | 9.22 | 45.06 | 6,299 | 284 | 30,785 | 197,006 | 31.28 |
| 35 | 7.62 | 11.73 | 56.98 | 6,015 | 343 | 29,218 | 166,221 | 27.63 |
| 40 | 9.41 | 14.49 | 69.92 | 5,672 | 396 | 27,370 | 137,003 | 24.15 |
| 45 | 12.93 | 19.91 | 94.83 | 5,276 | 500 | 25,128 | 109,633 | 20.78 |
| 50 | 16.20 | 24.95 | 117.43 | 4,775 | 560 | 22,475 | 84,505 | 17.70 |
| 55 | 23.48 | 36.16 | 165.81 | 4,215 | 699 | 19,326 | 62.030 | 14.72 |
| 60 | 32.58 | 50.17 | 222.89 | 3,516 | 784 | 15,620 | 42,704 | 12.15 |
| 65 | 41.84 | 64.43 | 277.46 | 2,732 | 758 | 11.766 | 27,084 | 9.91 |
| 70 | 73.63 | 113.39 | 1,000.00 | 1,974 | 1,974 | 15,318 | 15,318 | $7.76 \ddagger$ |
| B. FEMALES |  |  |  |  |  |  |  |  |
| 0 | 55.61 | (157.40) $\dagger$ | (139.84)* | 10,000 | 1,398 | 8,882 | 463,258 | 46.33 |
| 1 | 17.35 | 23.25 | 88.87 | 8,602 | 765 | 32,878 | 454,376 | 52.82 |
| 5 | 3.55 | 4.76 | 23.52 | 7,837 | 184 | 38,725 | 421,498 | 53.78 |
| 10 | 2.08 | 2.79 | 13.85 | 7,653 | 106 | 37,999 | 382,773 | 50.02 |
| 15 | 3.26 | 4.37 | 21.61 | 7,547 | 163 | 37,326 | 344,774 | 45.68 |
| 20 | 4.44 | 5.95 | 29.31 | 7,384 | 217 | 36,378 | 307,448 | 41.64 |
| 25 | 5.91 | 7.92 | 38.83 | 7,167 | 278 | 35,141 | 271,070 | 37.82 |
| 30 | 6.70 | 8.98 | 43.91 | 6,889 | 303 | 33,689 | 235,929 | 34.25 |
| 35 | 7.35 | 9.85 | 48.07 | 6,586 | 316 | 32,141 | 202,240 | 30.71 |
| 40 | 8.53 | 11.43 | 55.56 | 6,270 | 349 | 30,478 | 170,099 | 27.13 |
| 45 | 10.95 | 14.67 | 70.76 | 5,921 | 418 | 28,560 | 139.621 | 23.58 |
| 50 | 14.70 | 19.70 | 93.88 | 5,503 | 517 | 26,221 | 111,061 | 20.18 |
| 55 | 16.37 | 21.94 | 104.00 | 4,986 | 519 | 23,633 | 84,840 | 17.02 |
| 60 | 30.77 | 41.23 | 186.89 | 4,467 | 834 | 20,250 | 61,207 | 13.70 |
| 65 | 35.32 | 47.33 | 211.61 | 3,633 | 769 | 16,241 | 40,957 | 11.27 |
| 70 | 77.38 | 103.69 | 1,000.00 | 2,864 | 2,864 | 24,716 | 24,716 | $8.63 \ddagger$ |

* Estimated by linear interpolation on tables 'West' from the value of ${ }_{4} 4_{1}$.
$\dagger$ Computed from the formula $m_{0}=q_{0}\left(I . d l_{0}\right)$ where $L_{0}=0.2 I_{0}+0.8 l_{1}$.
$\ddagger$ Computed from Princeton life tables at a level corresponding to the level of $e_{1}$ (obtained by linear interpolation between two consecutive tables).

Madagascar. After 25 years of age, the male excess mortality in Madagascar is of the same order of magnitude as in Level 10 of the model life tables (Figure 3).

The calculation of the adjusted age-specific death rates also leads to an estimate of the true number of deaths, and thus to a determination of the overall rates of underregistration: about half of the males and over one-third of the female deaths are not registered. This method has, therefore, coped with defective vital statistics, yet the results obtained are fairly plausible (table 7).

Underregistration seems more pronounced for males than for females. This could well be true. Yet as the age of females at death may well be overstated at about age 50 (there is a marked tendency to overstate the age of highly fertile women), the index of concentration of deaths $i(1,50)$ may consequently be overestimated for females, leading then to an underestimation of the level of mortality at ages above one year.


Figure 2A. Location of Madagascar Mortality Rates within the Network of Princeton Life Tables (Model 'West')
These results also make it possible to estimate the crude death rate in the country. In Madagascar in 1965-67 these rates were per thousand

Males: 25.5
Females: 19.4
All: 22.4

## THE CASE OI: INAII:OUAC'Y OI: MODEI 'WI:ST'

As described previously, this method is valid wherever the age pattern of mortality in the country is fairly close to that of the model life tables selected as standard for the estimation of the death rate $m(a+)$.

The closeness of the two structures should, therefore, be checked. In the example of Madagascar, as shown in Figure 2, this relation seems quite satisfactory; the mortality rates in Madagascar deviate in a random manner around those of the 'West' table with the closest life-expectancy (Level 10 for males, 11 for females).


Figure 2B. Location of Madagascar Mortality Rates within the Network of Princeton Life Tables (Model 'West').
Contrariwise. in the case of Lebanon, the mortality rates obtained by using Model 'West' as a standard, deviate perceptibly from the patterns of this model. Mortality at older ages was that of a higher level in these model life tables than at younger ages. The selection of a more appropriate model was made by calculating comparative indices, which related the mortality rates in Lebanon to those of the model life tables with the same life expectancy in the four families (Table 8).

This trial and error approach is essential. The choice of Model 'West' for Madagascar only implied a level of mortality for the country. However, it yielded an estimate of the age-structure of this mortality. which was definitely independent of Model 'West' and based only upon the Madagascar data.

A comparison of the mortality rates, obtained for Lebanon by using Model 'West' as a standard, with those of the four Princeton families, showed that:
(1) For the same level of mortality (measured by the life expectancy at birth). mortality rates of Table 'West' were relatively higher at younger ages and lower at older ages than those of Lebanon;

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$$

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Figure 3. Excess male mortality indices.

Table 7. Rates of underregistration of deaths

| Agc | Registered deaths |  |  | Estimated deaths |  |  | Rate al underregistration (per cent) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Males | Females | All | Males | Iemales | AII | Males | lemales | AII |
| 0 | 8.604 | 7.340 | 15.944 | 29,284 | 20.776 | 50.060 | 71 | 65 | 68 |
| 1 and over | 31.391 | 30,108 | 61,499 | 48,342 | 40,345 | 88.687 | 35 | 25 | 31 |
| All ages | 39,995 | 37.448 | 77,443 | 77,626 | 61,121 | 138.747 | 48 | 39 | 44 |

Source: Registered deaths are taken from Table 1, rate of underregistration and estimated deaths taken from Table 5.
(2) Models 'North' and 'East' were even further from Lebanese mortality than Model 'West':
(3) Model 'South' seemed closest to Lebanese mortality as regarded by the age structure of deaths above age 5 . For the same life expectancy at birth, mortality was higher at ages below five in Table 'South' than in Lebanon and lower above this age. But the relative difference between the mortality in Model 'South' and that in Lebanon was about the same in the two age groups $5-59$ years and 60 years and over. Therefore, we conclude that Lebanese mortality showed the same pattern of variation by age as Model 'South' above the age of five years. ${ }^{19}$
The calculations should therefore be started again (in the same order as above) using now the

[^4]model closest to the age structure of deaths. In the case of Lebanon, the use of Model 'South' as standard for the estimation of mortality above five years of age has resulted in the mortality rates of Table 9. On Figure 4, it may be observed that the two curves of mortality rates obtained by using Models 'West' and 'South' respectively are parallel. ${ }^{20}$ This proves once again that this method helps only to locate a level of mortality, but that the structure of motality rates is independent of the selected model life tables.

Table 8. Comparison of mortality rates in Lebanon with those of the model life tables

| Age | Lebanese mortality rates (computed with Model 'West' as standard)* | Mortality rates in the model life tables ( $\%$ ) $\dagger$ |  |  |  | Comparative indices $\ddagger$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 'South' | 'North' | 'East' | 'West' | 'South' | 'North' | 'East' | 'West' |
| 0 | 57.97 | 81.88 | 53.33 | 71.77 |  |  |  |  |  |
| 1-4 | 20.98 | 30.86 | 28.32 | 18.44 | 56.52 20.35 | 1.412 | 0.920 | 1.238 | 0.975 |
| 5-9 | 8.76 | 6.37 | 13.00 | 18.44 6.58 | 20.35 | 1.471 | 1.350 | 0.879 | 0.970 |
| 10-14 | 6.33 | 4.52 | 13.05 | 6.58 4.74 | 7.51 5.81 | 0.727 | 1.484 | 0.751 | 0.857 |
| 15-19 | 7.52 | 6.64 | 11.27 | 4.74 7.95 | 5.81 9.22 | 0.714 | 1.272 | 0.749 | 0.918 |
| 20-24 | 10.14 | 9.35 | 115.54 | 7.95 1122 | 9.22 12.73 | 0.883 | 1.499 | 1.057 | 1.226 |
| 25-29 | 11.14 | 10.27 | 16.77 | 11.22 12.00 | 12.73 | 0.922 | 1.533 | 1.107 | 1.255 |
| 30-34 | 13.95 | 12.23 | 18.34 | 12.00 | 14.85 | 0.922 | 1.505 | 1.077 | 1.333 |
| 35-39 | 17.01 | 14.44 | 20.91 | 13.57 | 15.56 | 0.877 | 1.315 | 0.973 | 1.115 |
| 40-44 | 22.29 | 19.37 | 26.03 | 16.81 22.22 | 19.70 | 0.849 | 1.229 | 0.988 | 1.158 |
| 45-49 | 30.59 | 26.34 | 31.94 | 32.22 | 25.61 35.30 | 0.869 | 1.168 | 0.997 | 1.149 |
| 50-54 | 48.14 | 39.76 | 31.94 45.25 | 31.84 47.88 | 35.30 50.88 | 0.861 | 1.044 | 1.041 | 1.154 |
| 55-59 | 69.85 | 56.44 | 60.14 | 47.88 71.39 | 50.88 74.04 | 0.826 | 0.940 | 0.995 | 1.057 |
| 60-64 | 117.53 | 87.32 | 60.14 90.97 | 71.39 108.25 | 74.04 111.07 | 0.808 | 0.861 | 1.022 | 1.060 |
| 65-69 | 177.99 | 136.87 | 90.97 139.90 | 108.25 167.49 | 111.07 16642 | 0.743 | 0.774 | 0.921 | 0.945 |
| 70-74 | 248.99 | 224.84 | 139.90 215.87 | 167.49 261.94 | 166.42 | 0.769 | 0.786 | 0.941 | 0.935 |
| 75-79 | 367.91 | 366.07 | 326.34 | 261.94 394.40 | 252.23 373.43 | 0.903 | 0.867 | 1.052 | 1.013 |
|  |  | 366.07 | 326.34 | 394.40 | 373.43 | 0.995 | 0.887 | 1.072 | 1.015 |

Source: See Courbage and largues: loc. cit. in footnote 3, p. 17.

* This series of mortality rates has been obtained in using model 'West' as standard, provisionally
$\dagger$ Mortality rates for both sexes obtained by using the mortality rates for each sex in the model lif
the sex ratios by age of the Lebanese population, their mortality rates for cach sex in the model life tables and sexes (interpolated between two conseculive tan, their level being that corresponding to $\dot{e}_{0}=63.7$ years for both
$\ddagger$ Ratio of mortality rates in model life tables)

The reference to model life tables is perhaps not the best approach. Obviously, each set of model life tables summarizes the mortality experience of a large number of countries; thus, mortality in any one country may deviate, more or less, from all available models. So, the estimation of $m(a+)$ may well gain in precision if reference was to be made to the life tables of actual countries, rather than the Princeton models. Such sets of countries, should belong to a homogeneous geographical region containing the country studied. In Lebanon, we used this method as a first approach (Table 9 and Figures 4 and 5). It yielded results which were fairly close to those found subsequently by using model life tables. ${ }^{21}$ Actually, the use of data from real countries is questionable, because little is known as a rule about mortality conditions in the region studied. This is why we consider that the reference to model life tables is at present, an adequate substitute, especially as the choice of the actual model has limited influence on the final results.

[^5]

Figure 4. Mortality rates ohtained with various family of life tables as standard. Iebanon, 1970.
Table 9. Estimation of mortality rates in Lebanon (1970) using various familics of tables as standard (both sexes)

|  | Life tables selected as standard |  |  |
| ---: | ---: | ---: | ---: |
| Age | Princeton 'West' | Princeton 'South' | Set of countries |
|  |  |  |  |
| 0 | 57.97 | 65.10 | 64.50 |
| 1 | 20.98 | 22.23 | 22.51 |
| 5 | 8.76 | 7.92 | 9.45 |
| 10 | 6.33 | 5.73 | 6.88 |
| 15 | 7.52 | 6.78 | 8.07 |
| 20 | 10.14 | 8.76 | 10.89 |
| 25 | 11.14 | 9.85 | 12.11 |
| 30 | 13.95 | 12.94 | 14.86 |
| 35 | 17.01 | 14.97 | 19.01 |
| 40 | 22.29 | 20.70 | 25.94 |
| 45 | 30.59 | 27.12 | 32.16 |
| 50 | 48.14 | 43.75 | 63.86 |
| 55 | 69.85 | 62.92 | 81.38 |
| 60 | 117.53 | 104.13 | 142.09 |
| 65 | 177.99 | 163.84 | 208.25 |
| $e_{0}^{*}$ | 63.57 | 64.05 | 61.20 |

## Source: As Table 8.

* Life expectancy at birth derived from the combination of these rates.


Figure 5. Mortality level and age distribution of deaths in selected countries: (1) Cyprus (1950); (2) Greece (1963); (3) Italy (1964); (4) Spain (1960); (5) France (1965); (6) Puerto-Rico (1965); (7) Taiwan (1965); (8) Costa Rica (1963); (9) Ceylon (1963); (10) Singapore (1957); (11) Mexico (1965); (12) Chile (1960); (13) Ecuador (1962)

Calculation sheet of the death rate $m(a+)$ and of the correction factor $m(a+) / \mathrm{m}^{\prime}(a+)$

| Age | Population | Number of average deaths 1965-67 | Registered rates | ${ }_{a} P_{x}{ } m_{x}$ in different levels of Model 'West' tables |  |  |  |  |  |  |  |  |  |  | Interpolated rates | Correction factor |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $x, x+a$ | ${ }_{a} P_{x}$ | ${ }_{a} D_{x}$ | $a^{m^{\prime}{ }_{x}}$ | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |  | $\mathrm{m}^{\prime}(\mathrm{a}+$ |
| 0 | 133 | 8,604 | 64.69 | 48.995 | 44.018 | 39,590 | 35,617 | 32,032 | 28,773 | 25,797 | 23,072 | 20.454 | 18.071 | 16.005 |  |  |
| 1-4 | 432 | 7,753 | 17.95 | 21,669 | 19,423 | 17,392 | 15.548 | 13,859 | 12,308 | 10,873 | 9,547 | 8.027 | 6,756 | 5.707 |  |  |
| 5-9 | 484 | 1,798 | 3.71 | 4.646 | 4.230 | 3,848 | 3,494 | 3,165 | 2.860 | 2,570 | 2,304 | 2,013 | 1,767 | 1.549 |  |  |
| 10-14 | 428 | 934 | 2.18 | 2,936 | 2,679 | 2,444 | 2,221 | 2,016 | 1,823 | 1,644 | 1,477 | 1.288 | 1,138 | 1.006 |  |  |
| 15-19 | 269 | 876 | 3.26 | 2,531 | 2,319 | 2,122 | 1,939 | 1,770 | 1,611 | 1,463 | 1,323 | 1.192 | 1.068 | 958 |  |  |
| 20-24 | 193 | 779 | 4.04 | 2,600 | 2,378 | 2,175 | 1,986 | 1,812 | 1,648 | 1,496 | 1,353 | 1,220 | 1,092 | 979 |  |  |
| 25-29 | 163 | 903 | 5.54 | 2,461 | 2,248 | 2,051 | 1,870 | 1.700 | 1,544 | 1,397 | 1,258 | 1,131 | 1,009 | 898 |  |  |
| 30-34 | 156 | 934 | 5.99 | 2,733 | 2,493 | 2,271 | 2,069 | 1,880 | 1,703 | 1,540 | 1,387 | 1,245 | 1,262 | 983 |  |  |
| 35-39 | 154 | 1,173 | 7.62 | 3.175 | 2,900 | 2,646 | 2,410 | 2,193 | 1,991 | 1,803 | 1.628 | 1.465 | 1.309 | 1,169 |  |  |
| 40-44 | 133 | 1,251 | 9.41 | 3,332 | 3,047 | 2,785 | 2,546 | 2,324 | 2.117 | 1,925 | 1.745 | 1,576 | 1,420 | 1.282 |  |  |
| 45-49 | 125 | 1.616 | 12.93 | 3,654 | 3,361 | 3,092 | 2,845 | 2,616 | 2,404 | 2,206 | 2,021 | 1.846 | 1.694 | 1,556 |  |  |
| 50-54 | 106 | 1,717 | 16.20 | 3,954 | 3,653 | 3,377 | 3,124 | 2.891 | 2,674 | 2,473 | 2,285 | 2,101 | 1,953 | 1.818 |  |  |
| 55-59 | 84 | 1,972 | 23.48 | 3,861 | 3,595 | 3,352 | 3,131 | 2,926 | 2,736 | 2,559 | 2,396 | 2,234 | 2.109 | 1.992 |  |  |
| 60-64 | 60 | 1,955 | 32.58 | 3,801 | 3,553 | 3.328 | 3,121 | 2,932 | 2,756 | 2,594 | 2,444 | 2.298 | 2.185 | 2.080 |  |  |
| 65-69 | 51 | 2,134 | 41.84 | 4,356 | 4,096 | 3,860 | 3,644 | 3.447 | 3.266 | 3,097 | 2.941 | 2,792 | 2,677 | 2.570 |  |  |
| $70+$ | 76 | 5,596 | 73.63 | 11,562 | 11,167 | 10.812 | 10,489 | 10.194 | 9,920 | 9,667 | 9,429 | 9.203 | 9.023 | 8.852 |  |  |
| Total | 3,047 | 39,995 | 13.13 | 126,266 | 115,165 | 105.151 | 96,054 | 87,757 | 80,134 | 73,104 | 66,610 | 60.085 | 54.533 | 49.404 |  |  |
| $1+$ | 2,914 | 31,391 | 10.77 | 77,271 | 71,147 | 65,561 | 60.437 | 55,725 | 51,361 | 47.307 | 43.538 | 39.631 | 36.462 | 33.399 |  |  |
| $5+$ | 2.482 | 23,638 | 9.52 | 55.602 | 51,719 | 48.163 | 44.889 | 41,866 | 39,053 | 36.434 | 33,991 | 31.604 | 29,706 | 27.692 |  |  |
| $50+$ | 377 | 13,374 | - | 27.534 | 26,064 | 24,729 | 23,509 | 22.390 | 21.352 | 20.390 | 19.495 | 18.628 | 17.947 | 17,312 |  |  |
| $60+$ | 187 | 9,685 | - | 19.719 | 18.816 | 18.000 | 17,254 | 16,573 | 15.942 | 15,358 | 14.814 | 14.293 | 13.885 | 13.502 |  |  |
| i(1,50) | - | 0.4260 | - | 0.3563 | 0.3663 | 0.3772 | 0.3890 | 0.4013 | 0.4157 | 0.4310 | 0.4478 | 0.4700 | 0.4922 | 0.5183 | 16.62 | 1.54 |
| i(5.50) | - | 0.5658 | - | 0.4952 | 0.5040 | 0.5134 | 0.5237 | 0.5348 | 0.5467 | 0.5596 | 0.5735 | 0.5894 | 0.6042 | -0.6252 | 14.24 | 1.50 |
| i(1,60) | - | 0.3085 | - | 0.2552 | 0.2645 | 0.2746 | 0.2855 | 0.2974 | 0.3104 | 0.3246 | 0.3403 | 0.3607 | 0.3808 | 0.4043 | 17.85 | 1.66 |
| i(5.60) | - | 0.4097 | - | 0.3546 | 0.3638 | 0.3737 | 0.3844 | 0.3959 | 0.4082 | 0.4215 | 0.4358 | 0.4523 | 0.4674 | 0.5876 | 15.61 | 1.64 |
| t(1 +) |  | 10.78 |  | 26.52 | 24.42 | 22.50 | 20.74 | 19.12 | 17.63 | 16.23 | 14.94 | 13.60 | 12.51 | 11.46 |  |  |
| t( $5+$ ) |  | 9.52 |  | 22.40 | 20.84 | 19.40 | 18.09 | 16.87 | 15.73 | 14.68 | 13.70 | 12.73 | 11.97 | 11.16 |  |  |


[^0]:    * I'. Courbage and I'. Iargues are both Lecturers in Demography at IFORD (Institut de Forination et de Recherche Démographiques) in Yaoundé, Cameroon.
    ${ }^{1}$ A method for dealing with mortality was devised by Carrier, in 1958. ('A note on the estimation of mortality and other population characteristics, given deaths by apc', Population Shudic's 12, pp. 149-163). This method which assumes stability of the population studied may not given satisfactory results. For example, in Jordan (in 1951) the estimated crude death rate was 10.7 per cent, whereas it should have been close to, or even higher than, 20 per cent. See W. Brass, Mcthods for Estimating Mortality' from Limited and Defective Data (Chapel Hill: The North Carolina Population Centre, 1975).
    ${ }^{2}$ Brass, op. cit. in footnote 1.
    ${ }^{3}$ Y. Courbage and Ph. Fargues, Some Methodological Elements Proper to Lebanese Data in Order to Obtain Basic Indices on Mortality, UNESOB/WHO. Expert Group Meeting on Mortality (Beirut, 1972).
    ${ }^{4}$ Y. Courbage and Ph. Fargues, La simation demographique au liban, tome I (Bevrouth. 1973).
    ${ }^{5}$ Brass, op. cil. in loonnote 1 .
     tials in Somu Arali and African Countries (Cairo: Cairo Denographic (Centre, 1975).
    ${ }^{7}$ In the francophone countries of Africa, for instance, OCAM (Organisation Commune Africaine et Mauriciennc) and UDEA-Tchad (Union Douaniere et liconomique des Etats d'Afrique (entrale) have already established projects with the object of expanding and improving vital repistration.
    - This age could not exceed minimum school age.
    - We cannot truthfully state that the probability of a death being recorded is statistically independent of age. The many seasons for non-registration are still insufficiently known to establish a relation with the age of the deceased. On the other hand, it is not certain, cither, that the assumption is wrong. In our view the likeliloood is

[^1]:    "In the case of Lebanon, as the age structure was obtained from a sample survey, such an adjustment was thought necessary.

[^2]:    ${ }^{12}$ The values of the registered death rates in Madagascar for the open groups a + are as follow (per thousand):

[^3]:    ${ }^{17}$ Statistical publications frequently give infant deaths by day, week or month of age. When the structure of infant mortality in tropical regions is better known, the same method as that devised here for the study of mortality above one year could be used to estimate,$a_{0}$. The basis of this estimation would be the following observation: as infant mortality decreases, deaths tend to be more concentrated in the first days of life. A positive correlation should thus exist between $q_{0}$ and an index of concentration of infant deaths in the last months of the first year. Ihis index could be the ratio of deaths aged 3-11 months to the deaths aged 0-11 months.
    ${ }^{18}$. If, for example, underregistration of deaths were to increase with age, the mortality rates computed for Madagascar would all have been above the average level at younger ages and below it at older ages.

[^4]:    ${ }^{19}$ It is this closeness of the age structure of mortality in Lebanon above the age of five years to that of Model 'South' that justified the selection of $a=5$ years in the case of Lebanon.

[^5]:    ${ }^{20}$ Since $q_{0}$ and $q_{1}$ were estimated by another method, this parallelism is not observed at ages below five.
    ${ }^{21}$ The irregular deviations which appear on ligure 4 between the mortality rates obtained by this method and those obtained by using model life tables have come about because the age structure of the population was adjusted slightly in the second case but not in the first.

